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Investigation of electronic structure and optical properties of thallium lead halides: First principle calculations

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Using first principle calculations, we comprehend the electronic structure and optical constant of thallium lead halides TI3PbX5 (X = Cl, Br, I), which are viewed as potential materials for mid-infrared and near-infrared applications. The generalized gradient approximation function given by Perdew-Burke-Ernzerhof is used for geometry optimization and properties calculations. The calculated Mulliken charges are more positive for Pb than TI in the TI3PbCl5 system demonstrating a high electronic density contribution from the Pb-Cl bonds in contrast to the TI-Cl bonds. Similarly, the TI3PbCl5 configuration displays the smallest enthalpy value suggesting a more stable structure among different TI3PbX5 species studied in this work. The band gap value for TI3PbCl5 has been calculated as 3.52 eV, which decreases to 3.14 eV and 2.64 eV for the TI3PbBr5 and TI3PbI5, respectively. Additionally, the TI3PbI5 exhibits a high magnitude of real component of static dielectric function ε1(k) in contrast to TI3PbBr5 and TI3PbCl5. The optical absorption results display a redshift when TI3PbCl5 is doped with Br and I sequentially. These outcomes suggest that the concentration of halide elements can be adjusted to enhance the optical properties of TI3PbX5 for optoelectronic device applications. Published by AIP Publishing.

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I. INTRODUCTION

The progress in non-linear optical crystals for mid-infrared (MIR = 3–12 μm) laser sources provides widespread opportunities for applications in cutting edge technologies, such as space based communication systems, medical diagnostics, and remote sensing. The challenge with such materials is the scaling down of particle size so that it can be compacted in small volumes while considering characteristics such as hygroscopicity, stability, and energy/power output. Previously, rare-earth chlorides (i.e., Pr3+; LaCl3) lasing at 2.34 and 4.31 μm (Ref. 2) and chalcogenides (i.e., Dy3+; CaGa2S4) lasing at 3.2 and 7.2 μm (Ref. 3) have been considered as potential materials for MIR applications; however, these materials are exceedingly hygroscopic, which impede their usefulness in the development of laser sources. Therefore, an increasing attention has been given to synthesize new non-hygroscopic counterparts for MIR laser applications. Along these lines, thallium lead halides have shown remarkable potential for next generation optical and electrical applications. Thallium lead halide species with a stoichiometric formula of A3BX5 (A = TI; B = Pb; and X = Br, I, Cl) have emerged as new technological materials. These materials exhibit a perovskite (ABO3) crystal structure, which provide prospects to control their crystal morphology through processing and doping to achieve superior optical and electrical properties. In this manner, TI3PbBr5 and TI3PbCl5 have been studied for applications such as MIR and near-IR nonlinear optical effects. Likewise, rare-earth elements doped TI3PbBr5 has demonstrated an outstanding potency for MIR solid-state lasers. The presence of heavy lead ion in the crystal lattice structure of these materials is accounted for rendering hyper polarizability values. Additionally, it is predicted that the quantum dots of A3BX5 based perovskite structures have been barely studied. Initially, Keller9 studied the crystalline structure of TI3PbCl5 single crystal and calculated the cell parameters; however, the assigned space group (P41) was not confirmed by the latter’s work. Skarstad et al.10 synthesized single crystals of TI3PbCl5 using the Bridgman method and reported a non-centrosymmetric space group P41212 (No. 92), exhibiting a tetragonal symmetry containing four formula units per unit cell. This study has been further confirmed by X-ray single crystal diffraction measurements.11 Additionally, the first order phase transition of TI3PbCl5 has been reported as 155°C (Ref. 12) corresponding to the ordering of TI+ and Pb2+ cations leaving an unaffected position of Cl− anions. Another attempt was reported by Ferrier et al.11 who determined the phase transition temperature as 171°C for TI3PbCl4; however, they could not determine the exact phase transition temperature. Similarly, Khyzhun et al.13 studied the electronic structure and chemical stability of TI3PbBr5 single crystals grown by using the Bridgman-Stockalgar method. An X-ray photoelectron core-level and valence band (VB) spectrum were generated for the pristine and Ar− ions irradiated surfaces. Moreover, the total and partial density of

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states (PDOS) of the product materials were calculated using the full potential linearized augmented plane wave (FP_LAPW) based method. The low temperature (LT) TI$_3$PbBr$_5$ data suggested that Br 4p-like states dominated the VB contributing mainly to the top and central region of the VB. The TI 6s-and 6p-like states were observed to contribute in the bottom of the conduction band (CB).

Despite various studies directed on thallium lead halides, no study reports a detailed first principal investigation of the electronic microstructure and optical properties of TI$_3$PbX$_5$ analogs. In this paper, we have implemented first principle calculations to contemplate the electronic structure and optical properties of thallium lead halide species containing Cl, Br, and I. The geometric structures, formation energies, absorption properties, dielectric functions, and total and partial density of states have been analyzed to study the effect of varying the halide group in the host crystal structure of thallium lead halide.

II. COMPUTATIONAL DETAILS

The modeled structures of TI$_3$PbX$_5$ (X = Cl, Br, I) were optimized using first principal calculations. The generalized gradient approximation (GGA) function given by Perdew-Burke-Ernzerhof (PBE) was used to treat all electronic energy of exchange correlation for geometry optimization and properties calculations. Additionally, an ultrasoft pseudopotential and Broyden–Fletcher–Goldfarb–Shanno (BFGS) algorithm was utilized in all calculations. At first, the lattice parameters $a = 8.716\,\text{Å}$, $b = 9.241\,\text{Å}$, and $c = 15.687\,\text{Å}$ and $\alpha = \beta = \gamma = 90.000^\circ$ were used to build the TI$_3$PbCl$_5$ primitive cell using an orthorhombic crystal system exhibiting a space group of $P2_12_12_1$ (point group = 222). After geometry optimization, Cl was replaced with Br and I atoms sequentially to construct the TI$_3$PbBr$_5$ and TI$_3$PbI$_5$, respectively. A periodically repeated super cell $2 \times 2 \times 2$ large enough to approximate the physical properties was used for geometry optimization and properties calculations. The following convergence parameters were used to relax the structures and optical constant calculations including: (a) maximum force = 0.03 eV/atom, (b) energy tolerance factor = $1.0 \times 10^{-5}$ eV/atom, (c) maximum stress = 0.05 GPa, and (d) maximum displacement = 0.001 Å. We used an energy cut-off (340.0 eV) high enough to fully converge the properties and self-consistent function (SCF) $1.0 \times 10^{-6}$ eV/atom as the electron parameters. A $1 \times 1 \times 1$ k point sample set was used for geometry optimization and calculations of density of states. The electronic configurations used for the elements were TI: [Xe] 6s$^2$ 4f$^{14}$ 5d$^{10}$ 6p$^1$, Pb: [Xe] 4f$^{14}$ 5d$^{10}$ 6s$^2$ 6p$^2$, Cl: [Ne] 3s$^2$ 3p$^5$, Br: [Ar] 4s$^2$ 3d$^{10}$ 4p$^5$, and I: [Kr] 4d$^{10}$ 5s$^2$ 5p$^5$.

III. RESULTS AND DISCUSSION

A. Geometric structure

The geometrically optimized TI$_3$PbX$_5$ (X = Cl, Br, I) structure configurations are given in Figs. 1(a)–1(c). The corresponding lattice parameters, enthalpy, and Mullikan charges are given in Table I. A significant increment in the lattice parameters can be observed when the Cl is replaced by Br and I, which is related to the ionic radii of Br and I. The ionic radii of Br (1.96 Å) and I (2.2 Å) are larger in contrast to the ionic radius of Cl (1.81 Å). Subsequently, the substitution of Br and I successively expands the crystal lattice and hence increases the lattice parameters. The average Pb-halide bond length of 2.8933 Å has been calculated in the TI$_3$PbCl$_5$ crystal system. The corresponding average Pb-halide bond length for TI$_3$PbBr$_5$ and TI$_3$PbI$_5$ configurations increases to 2.9550 Å and 3.1606 Å, respectively, causing the cell to swell. In addition, we calculated the Mulliken charges to understand the electron density sheared by an atom in the TI$_3$PbX$_5$ crystal system. The more positive the Mulliken charge value is for an atom, the higher its electron density contribution is in the crystal system. The calculated Mulliken charge value for Pb is more positive compared to TI in the TI$_3$PbCl$_5$ crystal system suggesting more charge density contribution by Pb to form Pb-Cl bonds in contrast to TI-Cl bonds. Furthermore, no significant charge variation is observed for the Cl atoms in contrast to TI. Pb atoms lacking charge variation suggest that TI has a greater influence on altering the charge. A similar behavior is observed in the TI$_3$PbBr$_5$ and TI$_3$PbI$_5$ configurations. To compare the structure stability, we calculated enthalpy. The corresponding enthalpy values indicate that the geometric configuration of TI$_3$PbCl$_5$ is the most stable structure in all of the three TI$_3$PbX$_5$ species studied in this work.

![FIG. 1. Schematic of geometrically optimized structures of TI$_3$PbX$_5$ (X = Cl, Br, I) using GGA and PBE method.](image-url)

<table>
<thead>
<tr>
<th>Configuration</th>
<th>A (Å)</th>
<th>b (Å)</th>
<th>C (Å)</th>
<th>Enthalpy (eV)</th>
<th>Mullikan charges (Avg.)</th>
</tr>
</thead>
<tbody>
<tr>
<td>TI$_3$PbCl$_5$</td>
<td>8.4205</td>
<td>8.8401</td>
<td>15.1377</td>
<td>$-87954.8$</td>
<td>TI: 0.53, Pb: 0.90, Cl: -0.49, Br: ...</td>
</tr>
<tr>
<td>TI$_3$PbBr$_5$</td>
<td>8.7161</td>
<td>9.2413</td>
<td>15.6868</td>
<td>$-88768.7$</td>
<td>TI: 0.28, Pb: 0.52, Br: ...</td>
</tr>
<tr>
<td>TI$_3$PbI$_5$</td>
<td>9.1279</td>
<td>9.8622</td>
<td>16.6170</td>
<td>$-95412.4$</td>
<td>TI: 0.28, Pb: 0.42, Br: ...</td>
</tr>
</tbody>
</table>
B. Electronic properties

Figure 2 shows the calculated band structures and PDOS ranging from $-5$ to $5$ eV for the Tl$_3$PbX$_5$ ($X =$ Cl, Br, I) species with the Fermi level ($E_F$) set to 0. The results suggest significant variations in the band gap values corresponding to different halide elements in the structural models studied. The band gap value for Tl$_3$PbCl$_5$ is 3.52 eV, which decreases to 3.14 eV and 2.64 eV for Tl$_3$PbBr$_5$ and Tl$_3$PbI$_5$ configurations, respectively. The calculated band gap values are in good agreement with the experimental results.\(^{17}\) Generally, the density functional theory (DFT) calculations underestimate the band gap values due to termination of the DFT in GGA.\(^{18}\) However, such discrepancies can be corrected by using the Hubbard-like term ($U$) utilizing DFT + $U$ in order to treat the strong on-site Coulomb interaction of electrons that are underestimated by the local-density approximation (LDA) and GGA.\(^{19,20}\) The application of $U$ in DFT requires an expensive calculation time, which was unfortunately not available on our premises. Despite this drawback, the results can still be understood and the optical properties can be compared efficiently. A closer observation of the calculated band dispersion in Tl$_3$PbCl$_5$ for several symmetry directions suggests that the VB maxima (VBM) and CB minima (CBM) are not located at the same point which is characteristic of indirect band gap semiconductor materials. The Tl$_3$PbBr$_5$ and Tl$_3$PbI$_5$ configurations demonstrate a similar behavior. These results correlate with previously published works\(^{1}\) and references therein. It can be seen that the corresponding band structure is very dense with respect to energy, containing many electron states. A close observation of the VB suggests a weak band dispersion, which results in somewhat flat electronic bands. This behavior causes low mobility of holes. Moreover, the CB also demonstrates a narrow band distribution; however, it is more pronounced in comparison to the VB, indicating more electron mobility in the CB. Based on this, it can be inferred that the electron mobility in the CB is higher than the holes in the VB. This characteristic of materials is important for applications including light emitting diodes and solar cells.

The PDOS for various elements are given in Fig. 3 ranging from $-20$ to $20$ eV. The VB ranging from $-10$ to $0.3$ eV for Tl$_3$PbCl$_5$ can be divided into the upper VB ($-3.01$ to $0$ eV) and lower VB ($-3.01$ to $-10$ eV). The upper core TI-6p generates somewhat broader bands extending from 3.2 to 7.5 eV in the CB; however, the TI-6s demonstrates a narrow band in the VB and comparatively a broader band in the CB in the range of 8.2 to 18.7 eV. Similarly, Pb-6p (3.1 to 7.3 eV) and 6s (8.3 to 18.4 eV) like states generate broader bands in the CB and somewhat narrow bands in the VB. The TI-5d and Pb-5d like states develop sharp narrow bands in the lower VB region, while no significant contribution can be seen in the upper VB and CB. It can be noted that the Cl-3p states, Pb-6s states, and TI-6s states mainly contribute to the upper VB, while a small contribution can be traced from the TI-6s and Pb-6s like states in this region. However, no contribution is detected from the Cl-3s states. The TI-5d states contribute only in the lower VB at around $-10$ eV. Similarly, the TI-6p and Pb-5p like states mainly contribute to the CB, which extends in this region (3.25 $-$ 18.266 eV). Furthermore, the CB can be divided into lower CB (3.25 to 7.41 eV) and higher CB (8.33 to 17.87 eV). A small contribution from TI-6s and Pb-6s like states can also be traced in this region. Similar results were observed for Br and I containing configurations; however, Br-4s and I-5s demonstrate a significant contribution in the conduction band in contrast to Tl$_3$PbCl$_5$.

![FIG. 2. Calculated band structure, band gap energies, and total and partial densities of states for Tl$_3$PbX$_5$ (X = Cl, Br, I) using GGA and PBE method. The Fermi level is set to 0 eV on the energy axis as denoted by dotted red line.](image)
C. Optical properties

The optical constants are of high significance to outline materials showing superior optoelectrical properties for different applications including transparent conductive layers (TOCs),21,22 mid and near infra-red lasers,23 metal-semiconductor-insulator diodes,24 thin film transistors,25 and ultraviolet detectors.26 The interaction of photon with an electron in the ground state is depicted as the time dependent perturbation of the ground electronic state. The corresponding absorption or emission of photon causes the electronic transition between the occupied and vacant states. This excitation phenomenon produces a spectrum, which is considered as the joint density of states between the VB and CB.27 The complex dielectric function given in the following equation can be used to study the optical properties of materials:

\[\varepsilon(\omega) = \varepsilon_1 + i\varepsilon_2,\]  

(1)

where \(\varepsilon_1\) and \(\varepsilon_2\) are the real and imaginary components of dielectric functions, respectively, while \(\omega\) represents the photon frequency. The joint DOS and the momentum matrix function can be used to calculate the magnitude of \(\varepsilon_2(\omega)\) from the electronic structure using the following equation:28

\[\varepsilon_2(q \rightarrow \mathbf{q} \rightarrow \mathbf{q}) = \frac{2\pi e^2}{\Omega \delta_0} \sum_{\mathbf{k},\nu,\alpha} l(\psi_k^\nu | u, r | \psi_k^\nu)^2 \delta(E_k^\nu - E_k^\nu - E),\]  

(2)

where \(q\) is reciprocal lattice, \(u\) is incident electric field polarization, and \(v\) and \(c\) are valence and conduction bands, respectively. Along these lines, the Kramer-Kroning relation can be used to calculate the real part of dielectric function \(\varepsilon_1(\omega)\):

\[\varepsilon_1(\omega) = 1 + \frac{2}{\pi} \int_0^\infty \frac{\varepsilon_2(\omega)k^2}{\omega^2 - \omega^2} \, d\omega.\]  

(3)

Moreover, the other optical parameters including reflectivity \(R(\omega)\), refractive index \(n(\omega)\), dielectric loss function \(L(\omega)\), and absorption \(\alpha(\omega)\) properties are calculated using \(\varepsilon_1(\omega)\) and \(\varepsilon_2(\omega)\) values.29 The following equations are used to calculate the above-mentioned properties:

\[\alpha(\omega) = \frac{2}{\pi} \int_0^\infty \frac{\varepsilon_2(\omega)}{\omega^2 - \omega^2} \, d\omega,\]  

(4)

\[R(\omega) = \frac{(n - 1)^2 + k^2}{(n + 1)^2 + k^2},\]  

(5)

\[n(\omega) = \sqrt{\varepsilon_1^2(\omega) + \varepsilon_2^2(\omega) + \varepsilon_1(\omega)} \, \frac{1}{\sqrt{2}},\]  

(6)

\[L(\omega) = \frac{\varepsilon_2(\omega)}{(\varepsilon_1^2(\omega) + \varepsilon_2^2(\omega))},\]  

(7)

The calculated optical constants are given in Table II. The real and imaginary parts of the dielectric function are given in Fig. 4. The TI3PbI5 configuration demonstrates a high magnitude for \(\varepsilon_1(\omega)\) at zero frequency in contrast to TI3PbBr5 and TI3PbCl5 configurations. These results agree with the model proposed by Penn,17 suggesting an inverse

FIG. 3. The partial density of states for TI3PbX5 (X = Cl, Br, I) using GGA and PBE method demonstrating individual elements contributions in the valance and conduction band.
The magnitude of $\varepsilon_1(k)$ values is observed to increase, reaching a maximum value as 12.097 at 2.80 eV for TI3PbI5. A similar trend is detected for TI3PbBr5 and TI3PbCl5 at 10.25 (3.33 eV and 8.64) and 3.33 eV eV, respectively. The $\varepsilon_2(\omega)$ values, related to the optical absorption of materials, increase rapidly from the band gap values of 3.52, 3.14, and 2.64 eV for TI3PbX5 species doped with Cl, Br, and I, reaching a maximum at 5.17, 4.39, and 3.8 eV for Cl, Br, and I doped configurations, respectively. Additionally, the spectrum can be divided into three distinct peaks for all of the structural models. The lowest energy peaks (5.11, 4.39, and 3.77 eV for Cl, Br, and I, respectively) are related to the electronic transition from the upper VB to the lower CB. The second energy peaks at around 10.39, 9.42, and 7.92 eV (Cl, Br, and I, respectively) are consistent with the electronic transitions between the 3d- and 2p-states in the VB. The corresponding peaks significantly shifted to the low energy region for I. These results suggest that variation in the halide group of TI3PbX5 strongly influences their optical properties; hence, they can be used to manipulate these properties.

The energy loss function is given in Fig. 5, which demonstrates the energy lost by an electron accelerating through a material. Generally, the energy loss in the region to 50 eV is associated with plasmons while the energy loss beyond 50 eV is caused by excitations in the inner shell. The predominant peaks for Cl doped configuration appear at 4.05, 3.78, 1.86, and 1.09 eV for Cl, Br, and I doped configurations, respectively. These results suggest that the degree of order in pure Br doped configuration is the highest.

Figures 6(a) and 6(b) show the reflectivity and refractive index function of energy. The percentage of reflectivity for the I-doped configuration is high compared to Br and Cl doped configurations, which decrease significantly. The corresponding static reflectivity values are recorded as 0.143, 0.170, and 0.496 for Cl, Br, and I based models. The maximum reflectivity peaks at non-zero frequency are observed to be 4.99, 5.84, and 6.58 eV for I, Br, and Cl based configurations. Additionally, the reflectivity peaks are shifted to low photon energy for the I-doped model. The curve behavior for the $n(\omega)$ significantly varied for all of the TI3PbX5 species. It is clear from Fig. 6(b) that the $n(\omega)$ curves shift to low energy regions for Br and I doped configurations. Similar, an increase in the $n(\omega)$ is observed below the energy band gap values to a maximum value of 3.02, 3.28, and 3 at 4.11, 3.36, and 3.00 eV for Cl, Br, and I doped models. The corresponding static $n(\omega)$ and static $\varepsilon_1(k)$ values are related by equation: $n(\omega) = \sqrt{\varepsilon_1(\omega)}$, which are satisfied in our calculations for the TI3PbX5 models. The significant variation observed in $n(\omega)$ values by replacing halide groups provides an opportunity to manipulate the optical properties by doping different concentrations of thallium lead halides. Additionally, the variation is more pronounced in the low energy region in contrast to the high energy region. Therefore, it can be inferred that as the external pressure and phase transition is more pronounced in the low energy region.

<table>
<thead>
<tr>
<th>Configuration</th>
<th>$n(0)$</th>
<th>$\varepsilon_1(k)$</th>
<th>$L(\omega)\omega_p$</th>
<th>$R(0)$</th>
</tr>
</thead>
<tbody>
<tr>
<td>TI3PbCl5</td>
<td>2.22</td>
<td>4.91</td>
<td>2.29</td>
<td>0.143</td>
</tr>
<tr>
<td>TI3PbBr5</td>
<td>2.44</td>
<td>5.78</td>
<td>1.86</td>
<td>0.170</td>
</tr>
<tr>
<td>TI3PbI5</td>
<td>5.66</td>
<td>31.43</td>
<td>2.58</td>
<td>0.496</td>
</tr>
</tbody>
</table>

peak intensity generally corresponds to the order-disorder behavior of a crystal. In the current study, a high peak intensity is seen for TI3PbI5, which shows that iodine doping results in comparatively more disorder than Cl or Br doping. These results suggest that the degree of order in pure Br doped configuration is the highest.

FIG. 4. Calculated dielectric functions containing the real (a) and imaginary (b) components for TI3PbX5 (X = Cl, Br, I) configurations.

FIG. 5. Calculated loss-energy function for TI3PbX5 (X = Cl, Br, I) configurations.

FIG. 6. Calculated reflectivity (a) and refractive index (b) for TI3PbX5 (X = Cl, Br, I) configurations.
The absorption coefficient spectra (Fig. 7) for Ti₃PbX₅ show a wide absorption band starting at around the computed band gap values and increasing up to 34.6, 36.6, and 38.65 eV for Cl, I, and Br, respectively. The Ti₃PbCl₅ shows three distinct peaks around 6.48, 11.10, and 15.14, at 19.93, 26.52, and 33.04 eV, respectively. The peaks around 10 eV are called the vacuum ultraviolet region. It is clear that the replacement of Cl by Br and I significantly shifts the peaks to low energy. The results suggest a red shift, which is evident in the absorption versus frequency graph (inset figure of Fig. 7).

IV. CONCLUSIONS

In summary, we have applied the density functional theory to comprehend the electronic structure and optical properties of thallium lead halides in detail. The variation in halide elements from Cl to Br and I significantly affected the electronic band gap and optical properties of thallium lead halide crystal systems. The band gap was observed to decrease from 3.52 eV (Cl) to 3.14 eV (Br) and 2.64 eV (I). The calculated enthalpy values suggest that the Cl doped configuration is the most stable structure in contrast to Br and I doped configurations. The lattice parameters also demonstrate a significant increase by the addition of Br and I. The optical constant study suggests a variation in the low energy region. Based on this evidence, it can be inferred that by adjusting proper stoichiometric concentrations of the halide group elements (Cl, Br, and I), these elements can be used to manipulate the structure and therefore, the optical and electrical properties of these materials for practical device applications.