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## Effects of Y<sub>2</sub>O<sub>3</sub> on Sintering Behavior and Microwave Dielectric Properties of BiNbO<sub>4</sub> Ceramics

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 $Y_2O_3$  was selected as a substitute for  $Bi_2O_3$  and the effects of substitution on the sintering behavior and microwave dielectric properties of BiNbO<sub>4</sub> ceramics were studied. With the addition of 0.5 wt% CuO–V<sub>2</sub>O<sub>5</sub> mixtures, all  $Bi_{(1-x)}Y_xNbO_4$  ceramics could be densified below 900°C. The triclinic phases were identified in  $Bi_{(1-x)}Y_xNbO_4$  ceramics with x = 0.03 and the intensities of triclinic peaks increased with increasing x and sintering temperature. Saturated bulk density decreased from 7.17 g/cm<sup>3</sup> to 6.99 g/cm<sup>3</sup> and  $\varepsilon_r$  from 44.21 to 37.32 with increasing x from 0 to 0.1 for  $Bi_{(1-x)}Y_xNbO_4$  ceramics.  $Q \times f$  was mainly influenced by sintering temperature.  $\tau_f$  changed with x and sintering temperature. The  $\tau_f$  values of dense  $Bi_{(1-x)}Y_xNbO_4$  ceramics continuously decreased from 28.32 ppm/°C to -8.78 ppm/°C with the increase in x from 0 to 0.1. [DOI: 10.1143/JJAP.42.3514]

KEYWORDS: Bi(1-x)YxNbO4, microwave dielectric properties, low firing, microstructure, XRD patterns

### 1. Introduction

With the rapid progress in commercial wireless communication, the downsizing of mobile communication terminals has become increasingly important for convenience of use. Therefore, the components used in those terminals must also be miniaturized. The application of multilayer microwave devices will contribute to the realization of this goal.<sup>1)</sup> In the fabrication of multilayer microwave devices, low-firing microwave dielectric materials with high dielectric constant  $\varepsilon_{\rm r}$ , low dielectric loss and near-zero temperature coefficient of resonant frequency  $\tau_{\rm f}$  are necessary for co-firing with low-loss, low-melting-point conductors such as silver and copper. (Zr, Sn)TiO<sub>4</sub>, Ba<sub>2</sub>Ti<sub>9</sub>O<sub>20</sub>, and Ba(MgTa)O<sub>3</sub> systems have excellent microwave dielectric properties and are the most commonly used dielectric materials in ultra highfrequency applications.<sup>2-4)</sup> However, they are not compatible with the co-firing process because of their high sintering temperature. Low-melting-glass addition, chemical processing and use of small-particle sizes of the starting materials are three methods generally used in reducing the sintering temperature of dielectric materials.<sup>5-8)</sup> However, they also result in the deterioration of microwave dielectric properties, or require a flexible procedure. Furthermore, the sintering temperatures of those commercial dielectric materials using these methods are still too high for the use of lowmelting-point electrodes.

Bismuth-based dielectric ceramics are low-fired materials and have been investigated as materials of multilayer capacitors.<sup>9)</sup> Kagata et al. first studied the microwave dielectric properties of the Bi2O3-Nb2O5 system.<sup>10)</sup> Their results showed that BiNbO<sub>4</sub> ceramics with Cuo/V<sub>2</sub>O<sub>5</sub> addition could be densified at  $875^{\circ}$ C and had a Q of 4260 (at 4.3 GHz),  $\varepsilon_r$  of 43 and large  $\tau_f$  of 38 ppm/°C (-25-20°C). In order to lower  $\tau_f$ , Nd<sub>2</sub>O<sub>3</sub> and La<sub>2</sub>O<sub>3</sub> were substituted for Bi<sub>2</sub>O<sub>3</sub> and the effects of substitution on the densification and microwave dielectric properties of BiNbO4 ceramics were investigated by Choi et al. and Huang et al., respectively.<sup>11,12)</sup> For Nd or La substitution, the phase transition temperature (orthorhombic to triclinic) of BiNbO<sub>4</sub> ceramics decreased due to the lattice distortion caused by the ionic difference between  $Ln^{3+}$  (Ln = Nd, La) and  $Bi^{3+}$ . The  $Q \times f$  and  $\tau_f$  of Ln-modified BiNbO<sub>4</sub> ceramics were assumed to correlate with phase transformation ratio. The valence of Y<sup>3+</sup> is the same as that of Bi<sup>3+</sup> but its ionic radius (0.892 Å) is smaller than that of Bi<sup>3+</sup> (1.02 Å) or Nd<sup>3+</sup> (0.995 Å).<sup>13)</sup> Since the ionic difference between Ln<sup>3+</sup> and Bi<sup>3+</sup> plays an important role in the phase transition and microwave dielectric properties of Ln-modified BiNbO<sub>4</sub> ceramics, it motivated us to investigate the influence of Y substitution for Bi on the sintering behavior and microwave dielectric properties of BiNbO<sub>4</sub> ceramics. A small amount of CuO–V<sub>2</sub>O<sub>5</sub> mixture was used as sintering aids. The crystal-line phases and microstructures of the sintered specimens were also characterized.

### 2. Experimental

Samples of  $Bi_{(1-x)}Y_xNbO_4$  (x = 0, 0.01, 0.03, 0.05, 0.10) were prepared by conventional solid-state reaction methods. High-purity oxide powders,  $Bi_2O_3$  (>99.99%),  $Y_2O_3$ (>99.99%) and Nb<sub>2</sub>O<sub>5</sub> (>99.97%), were used as starting materials. These powders were mixed according to the desired stoichiometry and ball-milled for 24 h with deionized water in a nylon bottle with agate balls. The mixtures were dried and calcined at 800°C for 3 h. The calcined powders were mixed with a small amount of CuO-V<sub>2</sub>O<sub>5</sub> mixture (0.5 wt%) and then remilled for 24 h. After drying, the powders with 6 wt% PVA binder were uniaxially pressed into pellets in a steel die. The pellets were 16 mm in diameter and 7 mm in thickness. The pellets were sintered from 780°C to 900°C for 3 h. To prevent the vaporization of  $Bi_2O_3$ , the pellets were placed in a sealed alumina crucible filled with BiNbO<sub>4</sub> powder.

The bulk densities of the sintered ceramics were measured using the Archimedes method. The crystalline phases were identified based on X-ray diffraction patterns using Cu–K<sub> $\alpha$ </sub> radiation for 2 $\theta$  from 20 to 60° (Rigaku D/max 2550V X-ray diffractometer). The microstructural observation of the sintered surface of Bi<sub>(1-x</sub>)Y<sub>x</sub>NbO<sub>4</sub> ceramics was performed by scanning electron microscopy (SEM) (JEOL JSM-6700F). The average grain sizes were calculated by the line intercept method. Dielectric constant  $\varepsilon_r$  and quality value Qat the microwave frequency were measured using Hakki– Coleman's dielectric resonator method, as modified and improved by Courtney.<sup>14,15)</sup> An Advantest R3767CG network analyzer was employed in the measurement. The



Fig. 1. XRD patterns of  $Bi_{(1-x)}Y_xNbO_4$  ceramics with different *x* values sintered at different temperatures [\*: orthorhombic, o: triclinic].

temperature coefficient of the resonant frequency  $\tau_f$  was measured in the temperature range of  $-25^{\circ}C$  to  $+85^{\circ}C$ .  $\tau_f$  was defined as follows:

$$\tau_{\rm f} = \frac{f_{85} - f_{-25}}{110 \times f_{25}} \times 10^6 \quad (\rm ppm/^{\circ}C), \tag{1}$$

where  $f_{85}$ ,  $f_{-25}$  and  $f_{25}$  are the TE<sub>011</sub> resonant frequencies at 85°C,  $-25^{\circ}$ C and 25°C respectively.

### 3. Results and Discussion

Figure 1 shows the typical XRD patterns of  $Bi_{(1-x)}Y_xNbO_4$  ceramics with different x values sintered at different temperatures. Only the orthorhombic phase was revealed in the sintered BiNbO4 and Bi0.99Y0.01NbO4 ceramics, as shown in Figs. 1(a) and 1(b). However, for  $x \ge 0.03$ , orthorhombic and triclinic phases were found to coexist in sintered specimens and the triclinic peaks intensified with increasing Y content and sintering temperature. The orthorhombic phase, i.e., the low temperature phase of BiNbO<sub>4</sub>, is stable below 1020°C and then gradually transforms to the triclinic phase as the temperature increases.<sup>16,17)</sup> The existence of the triclinic phase proves that Y substitution could effectively lower the phase transition temperature. The lattice distortion caused by the ionic difference between  $Y^{3+}$  (0.892 Å) and  $Bi^{3+}$  (1.02 Å) appears to account for this result.<sup>11,12</sup> The phase transition temperature of Y-modified BiNbO4 ceramics is lower than that of Nd or La-modified BiNbO4 ceramics. This suggests that the large difference in ionic radius between  $Y^{3+}$  and  $Bi^{3+}$ induces more lattice distortion. However, the ratios (R) of  $I_{\rm tri}/[I_{\rm tri} + I_{\rm ortho}]$ , where  $I_{\rm tri}$  and  $I_{\rm ortho}$  are the intensities of triclinic (202),  $(\overline{2}10)$  and orthorhombic (040) reflection peaks of the XRD pattern, respectively,<sup>11,12)</sup> of  $Bi_{(1-x)}Y_xNbO_4$  ceramics with different x values at different sintering temperatures were all small. Even for x = 0.1 and sintering temperature of 900°C, the R of Y-modified BiNbO<sub>4</sub> ceramics was only 0.19. The amount of Y substitution for Bi was small (less than 0.1) and the phase transition of  $Bi_{(1-x)}Y_xNbO_4$  ceramics was limited when sintered at below 900°C for 3 h.

The densities of  $Bi_{(1-x)}Y_xNbO_4$  ceramics with different *x* values as a function of sintering temperature are shown in



Fig. 2. Bulk density of  $Bi_{(1-x)}Y_xNbO_4$  ceramics with x = 0-0.1 as a function of sintering temperature.

Fig. 2. The sintering temperatures of  $Bi_{(1-x)}Y_xNbO_4$  ceramics required for obtaining their maximum densities increased from 780°C to 900°C as x increased from 0 to 0.10. The increase of the coexisting amount of the triclinic phase in  $Bi_{(1-x)}Y_xNbO_4$  ceramics might account for this result because mass transportation in a sintering behavior is easily disturbed by second-phase generation. The densities of BiNbO<sub>4</sub> ceramics decreased from 7.17 g/cm<sup>3</sup> to 7.09 g/ cm<sup>3</sup> with increasing sintering temperature from 780°C to 860°C. For x = 0.01, the densities increased from 7.13 g/ cm<sup>3</sup> at 780°C to a maximum of 7.16 g/cm<sup>3</sup> at 800°C, and then slightly decreased with further increase in temperature. The saturated bulk densities of  $Bi_{(1-x)}Y_xNbO_4$  ceramics decreased from 7.17 g/cm<sup>3</sup> to 6.99 g/cm<sup>3</sup> with the increase in x from 0 to 0.10 owing to the substitution of heavier Bi atoms by lighter Y atoms.

The SEM images of  $Bi_{(1-x)}Y_xNbO_4$  ceramics with x = 0.01, 0.03, 0.05 and 0.1 sintered at different temperatures are shown in Fig. 3. The grain morphology of the Bi<sub>0.99</sub>Y<sub>0.01</sub>NbO<sub>4</sub> ceramic sintered at 780°C was uniform and distinct, as shown in Fig. 3(a1). The average grain sizes remained almost unchanged for the Bi0.99 Y0.01 NbO4 ceramic with increasing sintering temperature from 780°C to 800°C, an abnormal grain growth, which exhibited large discontinuous grains existing in a fine-grained matrix, could be observed with further increase in sintering temperature to 820°C [Figs. 3(a2) and 3(a3), respectively]. For the Bi<sub>0.97</sub>Y<sub>0.03</sub>NbO<sub>4</sub> ceramic sintered at 780°C, the as-sintered surfaces were porous and the grains did not grow [Fig. 3(b1)]. The pores were still easily observed on the surfaces of the Bi<sub>0.97</sub>Y<sub>0.03</sub>NbO<sub>4</sub> ceramic as-sintered at 800°C [shown in Fig. 3(b2)]. This suggests that the substitution of Y for Bi reduces the sinterability of BiNbO4 ceramics, as shown in Fig. 2. The number of pores decreased and the grain size increased with increasing sintering temperature from 800°C to 840°C for Bi<sub>0.97</sub>Y<sub>0.03</sub>NbO<sub>4</sub> ceramics [Figs. 3(b3) and 3(b4)]. The average grain sizes of dense  $Bi_{(1-x)}Y_xNbO_4$ ceramics (the samples reached their maximum relative densities) with various x values sintered at different temperatures, i.e., 800°C for x = 0.01 [Fig. 3(a2)], 840°C for x = 0.03 [Fig. 3(b4)], 860°C for x = 0.05 [Fig. 3(c)] and 900°C for x = 0.1 [Fig. 3(d)], ranged from approximately



(a1)

(a2)





Fig. 3. SEM images of  $Bi_{(1-x)}Y_xNbO_4$  ceramics for x = 0.01 sintered at (a1) 780°C, (a2) 800°C and (a3) 820°C; for x = 0.03 sintered at (b1) 780°C, (b2) 800°C, (b3) 820°C and (b4) 840°C; for x = 0.05 sintered at (c) 860°C; and for x = 0.1 sintered at (d) 900°C.



Fig. 4. Dielectric constant of  $Bi_{(1-x)}Y_xNbO_4$  ceramics with x = 0-0.1 as a function of sintering temperature.

0.98 to 1.11 µm. This means that Y substitution for Bi has no effect on the grain growth of the well-sintered  $Bi_{(1-x)}Y_xNbO_4$  ceramics.

Figure 4 shows the plots of the dielectric constant of  $Bi_{(1-x)}Y_xNbO_4$  ceramics as a function of sintering temperature for various x values. The  $\varepsilon_r$  of BiNbO<sub>4</sub> ceramics decreased from 44.21 to 40.99 with increasing sintering

temperature from 780°C to 860°C. The  $\varepsilon_r$  of  $Bi_{(1-x)}Y_xNbO_4$ ceramics with x ranging from 0.01 to 0.1 first increased with sintering temperature and saturated at 800°C-900°C depending on x, then decreased with further increase in sintering temperature. The relationship between sintering temperature and  $\varepsilon_r$  was found to be the same as that between sintering temperature and density. The increase in  $\varepsilon_r$  with sintering temperature is due to the well-known effects of grain growth and reduced porosity (the dielectric constant of pore equals 1.0). The decrease in  $\varepsilon_r$  above the densification temperature is associated with abnormal grain growth and increasing porosity, as shown in Fig. 3. It was found that  $\varepsilon_r$ of Bi<sub>(1-x)</sub>Y<sub>x</sub>NbO<sub>4</sub> ceramics also correlate to x. Saturated  $\varepsilon_r$ decreased with increasing Y content. For pure BiNbO<sub>4</sub> ceramics doped with 0.5 wt% CuO-V<sub>2</sub>O<sub>5</sub> mixture,  $\varepsilon_r$  could reach 44.21 at a sintering temperature of 780°C. However the  $\varepsilon_r$  of Bi<sub>0.9</sub>Y<sub>0.1</sub>NbO<sub>4</sub> ceramics sintered at 900°C critically decreased to 37.32. At microwave frequencies the dielectric constant of the ceramics is closely related to the sum of electronic and ionic polarizabilities of components. According to the ionic polarizabilities reported by Shannon, the polarizability of  $Y^{3+}$  (3.81) is smaller than that of Bi<sup>3+</sup> (6.12).<sup>18)</sup> Furthermore, the amount of triclinic phase  $\beta$ -BiNbO<sub>4</sub> increased with the increase in the amount of Y substitution for Bi in  $Bi_{(1-x)}Y_xNbO_4$  ceramics. The unit cell volume of  $\beta$ -BiNbO<sub>4</sub> is known to be smaller than that of  $\alpha$ -



Fig. 5.  $Q \times f$  of Bi<sub>(1-x)</sub>Y<sub>x</sub>NbO<sub>4</sub> ceramics with x = 0-0.1 as a function of sintering temperature.

BiNbO<sub>4</sub> (i.e.,  $V_{\beta\text{-BiNbO4}} = 324.0 \text{ Å}^3$  and  $V_{\alpha\text{-BiNbO4}} = 330.9 \text{ Å}^3$ ).<sup>16)</sup> The decrease in unit cell volume promotes the shrinkage of the octahedral and decreases the ionic polarizabilities of BiNbO<sub>4</sub>. Thus the saturated  $\varepsilon_r$  of Bi<sub>(1-x)</sub>Y<sub>x</sub>NbO<sub>4</sub> ceramics decreases with increasing Y content.

Figure 5 illustrates the  $Q \times f$  of  $Bi_{(1-x)}Y_xNbO_4$  ceramics as a function of sintering temperature. The  $Q \times f$  values of all samples increased with increasing sintering temperature. After reaching their maximum, the  $Q \times f$  values decreased slightly. Many factors are believed to affect microwave dielectric loss, which can be classified into two types, i.e., intrinsic loss and extrinsic loss.<sup>19)</sup> Intrinsic loss is caused by an anharmonic phonon decay process in a pure crystal lattice while extrinsic loss is caused by the existence of crystal defects, grain boundaries, second phases and pores.<sup>20)</sup> The densities and grain sizes of  $Bi_{(1-x)}Y_xNbO_4$  ceramics increased with increasing sintering temperature and then the number of pores and grain boundary areas decreased, which meant less lattice imperfections and lower dielectric loss. Abnormal grain growth, which occurred in sintered  $Bi_{(1-x)}Y_xNbO_4$  ceramics with further increase in sintering temperatures above the densification temperatures, led to the increase in the extent of crystal defects and the decrease in  $Q \times f$ . Choi *et al.* suggested that the  $Q \times f$  of BiNbO<sub>4</sub> ceramics rapidly increases as the triclinic transition ratio (R)is between 0.4 and 0.6 with Nd substitution for Bi.<sup>11</sup> Huang et al. found that  $Q \times f$  of BiNbO<sub>4</sub> ceramics appears to increase with increasing grain size for a given R with La substitution for Bi.<sup>12)</sup> The R of Y-modified BiNbO<sub>4</sub> ceramics was less than 0.2 in this experiment. The saturated  $Q \times f$  of  $Bi_{(1-x)}Y_xNbO_4$  ceramics decreased from 11483 GHz to 10480 GHz with increasing x from 0 to 0.03, and then increased to  $12814 \,\text{GHz}$  with further increase in x to 0.1. From the results of XRD patterns, we observed no triclinic phase (for x = 0, 0.01) or the R was very small (0.017 for x = 0.03 sintered at 840°C). The decrease in the  $Q \times f$  of  $Bi_{(1-x)}Y_xNbO_4$  ceramics with increasing x from 0 to 0.03 might arise from substitutional impurity effects, which enhance the anharmonicity of phonon vibrations.<sup>21-23)</sup> However, the increase in saturated  $Q \times f$  with further increase in x from 0.03 to 0.1 might be related to the increase in the intensity of triclinic phase. The maximum  $Q \times f$ 



Fig. 6.  $\tau_{\rm f}$  of Bi<sub>(1-x)</sub>Y<sub>x</sub>NbO<sub>4</sub> ceramics with x = 0-0.1 as a function of sintering temperature.



Fig. 7.  $\tau_f$  of dense Bi<sub>(1-x)</sub>Y<sub>x</sub>NbO<sub>4</sub> ceramics as a function of x.

could be obtained when *R* ranged between 0.03 and 0.06 in Y-modified BiNbO<sub>4</sub> ceramics with CuO–V<sub>2</sub>O<sub>5</sub> mixture addition.

The  $\tau_f$  values of  $Bi_{(1-x)}Y_xNbO_4$  ceramics with various x values at different sintering temperatures are shown in Fig. 6.  $\tau_f$  was influenced by sintering temperature. Compared with Fig. 4 and Fig. 6, the change in  $\tau_f$  with sintering temperature was in accordance with the change in  $\varepsilon_r$  with sintering temperature.  $\tau_f$  is related to the temperature coefficient of dielectric constant  $\tau_{\varepsilon}$  and that of linear expansion  $\alpha_L$  by<sup>24)</sup>

$$\tau_{\rm f} = -\tau_{\varepsilon}/2 - \alpha_{\rm L} \tag{2}$$

 $\alpha_{\rm L}$  is nearly constant for well-sintered ceramics. Thus,  $\tau_{\rm f}$  depends only on  $\tau_{\varepsilon}$ , which generally increases with increasing dielectric constant  $\varepsilon_{\rm r}$ . The change in  $\tau_{\rm f}$  with sintering temperature for a given *x* value was caused by the change in  $\varepsilon_{\rm r}$ , as shown in Fig. 4. Figure 7 shows the  $\tau_{\rm f}$  of dense  ${\rm Bi}_{(1-x)} Y_x {\rm NbO_4}$  ceramics as a function of *x*. The  $\tau_{\rm f}$  continuously decreased from 28.32 ppm/°C to -8.78 ppm/°C with increasing *x* from 0 to 0.1. This implies that  $\tau_{\rm f}$  can be adjusted to near zero by substituting a suitable amount of Bi with Y in BiNbO<sub>4</sub> ceramics.

### 4. Conclusions

The microstructure and the microwave dielectric proper-

ties of  $Bi_{(1-x)}Y_xNbO_4$  ceramics doped with 0.5 wt% CuO-V2O5 mixture were investigated. The phase transition temperature of BiNbO4 ceramics was reduced to below 900°C by the substitution of Y for Bi. The densification temperatures increased from 780°C to 900°C with increasing x from 0 to 0.1. Bulk density and  $\varepsilon_r$  increased with sintering temperature, reached their maximum values and then decreased with further increase in temperature. The saturated bulk density and  $\varepsilon_r$  of  $Bi_{(1-x)}Y_xNbO_4$  ceramics decreased with increasing of x.  $Q \times f$  was dependent on sintering temperature.  $\tau_{\rm f}$  was also dependent on sintering temperatures and x. A near zero  $\tau_{\rm f}$  could be obtained by carefully adjusting Y content. The  $Bi_{(1-x)}Y_xNbO_4$  ceramics with x =0.05 sintered at 860°C showed good microwave dielectric properties of  $\varepsilon_{\rm r} \sim 41.58$ ,  $Q \times f \sim 11579 \,{\rm GHz}$  and  $\tau_{\rm f} \sim$ 8.93 ppm/°C.

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